

# Galileo's inclined plane: $d \propto t^2$

FizziQ activity · High school · 30 min



Scan to open in FizziQ

Students reproduce Galileo's experiment in the FizziQ Web inclined plane simulation, plotting  $d$  versus  $t^2$  to extract acceleration and  $g$ . High school, browser.

## Learning objectives

- Experimentally verify the relationship  $d = \frac{1}{2} \times a \times t^2$  on an inclined plane
- Measure the acceleration of a ball for different inclination angles
- Verify the relationship  $a = g \times \sin(\alpha)$
- Plot and interpret  $d$  versus  $t^2$  graphs to extract the acceleration
- Determine the value of  $g$  from the slope of the  $a$  versus  $\sin(\alpha)$  graph

## Instruments and sensors

FizziQ Web Inclined Plane simulation

## Materials

- Computer, tablet, or smartphone with FizziQ Web
- Note: the protocol remains adaptable to any comparable simulation or data-analysis tool.

## Protocol

1. Open the Inclined Plane simulation in FizziQ Web (Experiment → Simulations → Inclined Plane).
2. Set the inclination angle to  $30^\circ$  and the travel distance to maximum. Start a recording (REC) and let the ball roll to the bottom.
3. The position-time data are automatically exported to the experiment notebook. Observe the graph: the curve is not a straight line but a parabola.
4. Add a calculated column to the table:  $t^2$  (time squared). Plot the graph of distance versus  $t^2$ . This should be a straight line through the origin.
5. The slope of this line equals  $\frac{1}{2} \times a$ . Calculate the acceleration  $a$  for the  $30^\circ$  angle. Note the value in a summary table.
6. Repeat the experiment for angles  $10^\circ$ ,  $20^\circ$ ,  $40^\circ$ ,  $50^\circ$ , and  $60^\circ$ . For each angle, calculate the acceleration from the slope of  $d(t^2)$ .
7. Create a summary table with three columns: Angle,  $\sin(\text{angle})$ , and Acceleration.
8. Plot the graph of Acceleration versus  $\sin(\text{angle})$ . The curve should be a straight line through the origin.
9. The slope of this line gives the value of  $g$ . Compare your value with  $9.81 \text{ m/s}^2$ .
10. What happens at an angle of  $90^\circ$ ? The acceleration should equal  $g$ : that is free fall!

## Expected results

The  $d(t)$  graph is a parabolic curve, confirming non-uniform motion. The  $d(t^2)$  graph is a straight line through the origin, confirming  $d = \frac{1}{2} \times a \times t^2$ . The acceleration increases with angle: approximately  $1.7 \text{ m/s}^2$  at  $10^\circ$ ,  $4.9 \text{ m/s}^2$  at  $30^\circ$ , and  $8.5 \text{ m/s}^2$  at  $60^\circ$ . The graph  $a(\sin \alpha)$  is a straight line through the origin with slope  $g \approx 9.81 \text{ m/s}^2$ . The mass of the ball does not affect the results.

## Questions

- Why is the position-time graph a curve and not a straight line?

- What does the slope of the  $d(t^2)$  graph represent?
- Why does the acceleration not depend on the mass of the ball?
- If you double the angle from  $15^\circ$  to  $30^\circ$ , does the acceleration double?
- What would change if there were friction between the ball and the plane?
- At what angle is the acceleration exactly half of  $g$ ?

### Going further

- Plot  $v(t)$  for a given angle and verify that velocity increases linearly with time
- Compare the times to travel the same distance at two different angles
- Predict the acceleration for a new angle before measuring it, then check your prediction
- Add friction in the simulation (if available) and observe how the acceleration changes
- Determine the value of  $g$  by using only two different angles